

Introduction to the pageRank Package

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1 Introduction

1.1 Background

The *pageRank* package provides implementations of temporal PageRank as defined by [1], as well as multiplex PageRank as defined by [2]. As the extension of original steady-state PageRank [3,4] in temporal networks, temporal PageRank ranks nodes based on their connections that change over time. Multiplex PageRank, on the other hand, extends PageRank analysis to multiplex networks. In such networks, the same nodes might interact with one another in different layers. Multiplex PageRank is calculated according to the topology of a predefined

base network, with regular PageRank of other supplemental networks as edge weights and personalization vector.

PageRank-related approaches can be applied to prioritize key transcriptional factors (TFs) in gene regulatory networks (GRNs). Specifically, the *pageRank* package provides functions for generating temporal GRNs from corresponding static counterparts. The *pageRank* package also provides functions for converting multi-omics, e.g. gene expression, chromatin accessibility and chromosome conformation profiles to multiplex GRNs. Such temporal and multiplex GRNs can thus be used for temporal and multiplex PageRank-based TF prioritization, respectively.

1.2 Installation

pageRank requires the R version 4.0 or later, packages *BSgenome.Hsapiens.UCSC.hg19*, *TxDb.Hsapiens.UCSC.l*
org.Hs.eg.db, *annotate*, *GenomicFeatures*, *JASPAR2018*, *TFBSTools* and *bcellViper*, to run the examples. After installing R, all required components can be obtained with:

```
if (!requireNamespace("BiocManager", quietly=TRUE)) install.packages("BiocManager")
BiocManager::install("BSgenome.Hsapiens.UCSC.hg19")
BiocManager::install("TxDb.Hsapiens.UCSC.hg19.knownGene")
BiocManager::install("org.Hs.eg.db")
BiocManager::install("annotate")
BiocManager::install("GenomicFeatures")
BiocManager::install("JASPAR2018")
BiocManager::install("TFBSTools")
BiocManager::install("bcellViper")
```

2 PageRank Analysis

2.1 Temporal PageRank

We applied `diff_graph()` to calculate temporal PageRank. This is a simplified version of temporal PageRank described by [1] by only analyzing temporally adjacent graph pairs.

```
> library(pageRank)
> set.seed(1)
> graph1 <- igraph::erdos.renyi.game(100, 0.01, directed = TRUE)
> igraph::V(graph1)$name <- 1:100
> #the 1st graph with name as vertex attributes
> set.seed(2)
> graph2 <- igraph::erdos.renyi.game(100, 0.01, directed = TRUE)
> igraph::V(graph2)$name <- 1:100
> #the 2nd graph with name as vertex attributes
> diff_graph(graph1, graph2)
```

```

IGRAPH 46a8baf DN-- 98 190 --
+ attr: name (v/c), pagerank (v/n), moi (e/n)
+ edges from 46a8baf (vertex names):
  [1] 1 ->60  2 ->15  2 ->57  3 ->10  3 ->16  3 ->84  4 ->43  5 ->20  5 ->60
 [10] 5 ->72  5 ->81  5 ->91  6 ->25  6 ->50  7 ->37  7 ->67  7 ->73  7 ->80
 [19] 8 ->80  9 ->90 10->26 11->6  11->100 12->70 12->82 12->92 13->30
 [28] 13->48 13->51 13->61 15->74 15->77 16->85 17->31 17->32 17->30
 [37] 17->50 17->58 19->17 19->96 20->23 20->79 20->87 21->41 21->40
 [46] 22->4  22->41 23->57 24->61 25->66 26->34 26->39 26->72 27->20
 [55] 27->43 28->98 29->95 30->84 32->49 33->10 34->16 34->99 35->80
 [64] 36->17 36->33 36->45 36->53 36->77 37->33 37->54 38->6  38->10
+ ... omitted several edges

```

Differential graph graph1-graph2 will be outputed. The Differential graph has "moi (mode of interaction, 1 and -1 for interactions gained and lost in graph1, respectively)" as edge attribute. The Differential graph has "pagerank" and "name" as vertex attributes.

2.2 Multiplex PageRank

We applied `multiplex_page_rank()` to calculate multiplex PageRank following definition by [2].

```

> set.seed(1)
> graph1 <- igraph::erdos.renyi.game(100, 0.01, directed = TRUE)
> igraph::V(graph1)$name <- 1:100
> igraph::V(graph1)$pagerank <- igraph::page_rank(graph1)$vector
> #the base graph with pagerank and name as vertex attributes.
> set.seed(2)
> graph2 <- igraph::erdos.renyi.game(100, 0.01, directed = TRUE)
> igraph::V(graph2)$name <- 1:100
> igraph::V(graph2)$pagerank <- igraph::page_rank(graph2)$vector
> #the supplemental graph with pagerank and name as vertex attributes.
> multiplex_page_rank(graph1, graph2)

```

1	2	3	4	5	6
0.024486930	0.003587882	0.003269234	0.025062625	0.002517812	0.014031152
7	8	9	10	11	12
0.019560780	0.002517812	0.010657975	0.024750578	0.003587882	0.002517812
13	14	15	16	17	18
0.002517812	0.002517812	0.012543315	0.011993811	0.011752012	0.002517812
19	20	21	22	23	24
0.002517812	0.005019851	0.005073934	0.019579420	0.010917862	0.006654581
25	26	27	28	29	30

0.008481052	0.024875556	0.018813575	0.012145212	0.002517812	0.005371332
31	32	33	34	35	36
0.028390794	0.003870287	0.022958947	0.007132217	0.026500261	0.014220612
37	38	39	40	41	42
0.003894189	0.014025489	0.007048515	0.006489236	0.009884435	0.011620308
43	44	45	46	47	48
0.021776702	0.005804823	0.007274354	0.005973955	0.002517812	0.003231192
49	50	51	52	53	54
0.008363678	0.018470262	0.007252872	0.007734145	0.007333127	0.008132101
55	56	57	58	59	60
0.002517812	0.009882306	0.012570845	0.005099961	0.009773330	0.005728022
61	62	63	64	65	66
0.008887585	0.009392001	0.002517812	0.012318772	0.002517812	0.012403356
67	68	69	70	71	72
0.003894189	0.008046953	0.006637398	0.012164635	0.004952221	0.025846022
73	74	75	76	77	78
0.007717015	0.017071807	0.004497441	0.031878419	0.006205317	0.006125093
79	80	81	82	83	84
0.007674159	0.004657952	0.036708345	0.004133414	0.003587882	0.008317756
85	86	87	88	89	90
0.019805589	0.003587882	0.010071696	0.003779210	0.002517812	0.010708381
91	92	93	94	95	96
0.009826976	0.006014406	0.020117463	0.010635582	0.006048082	0.004657952
97	98	99	100		
0.012988768	0.015761377	0.004243860	0.003249976		

Multiplex PageRank values corresponded to nodes in graph1 (base network) will be outputed.

2.3 Adjusting PageRank Calculations

The `clean_graph()` can remove nodes by residing subgraph sizes, vertex names and PageRank values. We thus can adjust graphs for PageRank calculation.

```
> set.seed(1)
> graph <- igraph::erdos.renyi.game(100, 0.01, directed = TRUE)
> igraph::V(graph)$name <- 1:100
> igraph::V(graph)$pagerank <- igraph::page_rank(graph)$vector
> #the graph to be cleaned, with pagerank and name as vertex attributes.
> clean_graph(graph, size=5)
```

```
IGRAPH 9913984 DN-- 82 96 -- Erdos-Renyi (gnp) graph
+ attr: name (g/c), type (g/c), loops (g/l), p (g/n), name (v/n),
| pagerank (v/n)
```

```
+ edges from 9913984 (vertex names):
[1] 72-> 1 88-> 3 22-> 4 11-> 6 65-> 6 87-> 6 60-> 7 85->
[9] 84-> 9 33-> 10 100-> 10 11->100 2-> 15 40-> 15 3-> 16 34->
[17] 19-> 17 46-> 17 5-> 20 69-> 20 100-> 20 92-> 21 27-> 22 83->
[25] 42-> 24 6-> 25 10-> 26 74-> 27 94-> 27 43-> 31 36-> 33 38->
[33] 59-> 35 90-> 35 60-> 36 70-> 36 53-> 38 26-> 39 46-> 40 88->
[41] 21-> 41 71-> 41 49-> 42 65-> 42 77-> 42 87-> 43 100-> 43 52->
[49] 21-> 45 54-> 46 32-> 49 92-> 49 6-> 50 17-> 50 43-> 52 54->
+ ... omitted several edges
```

Adjusted graph will be outputted, with "pagerank" and "name" as vertex attributes.

The `adjust_graph()` can re-calculate PageRank with updated damping factor, personalized vector and edge weights.

```
> set.seed(1)
> graph <- igraph::erdos.renyi.game(100, 0.01, directed = TRUE)
> igraph::V(graph)$name <- 1:100
> igraph::V(graph)$pagerank <- igraph::page_rank(graph, damping=0.85)$vector
> #the graph to be adjusted, with pagerank and name as vertex attributes.
> adjust_graph(graph, damping=0.1)
```

```
IGRAPH 4694ffe DN-- 100 98 -- Erdos-Renyi (gnp) graph
+ attr: name (g/c), type (g/c), loops (g/l), p (g/n), name (v/n),
| pagerank (v/n)
+ edges from 4694ffe (vertex names):
[1] 72-> 1 88-> 3 22-> 4 11-> 6 65-> 6 87-> 6 60-> 7 85->
[9] 84-> 9 33-> 10 100-> 10 11->100 2-> 15 40-> 15 3-> 16 34->
[17] 19-> 17 46-> 17 5-> 20 69-> 20 100-> 20 92-> 21 27-> 22 83->
[25] 42-> 24 6-> 25 10-> 26 74-> 27 94-> 27 63-> 30 43-> 31 36->
[33] 38-> 35 59-> 35 90-> 35 60-> 36 70-> 36 53-> 38 26-> 39 46->
[41] 88-> 40 21-> 41 71-> 41 49-> 42 65-> 42 77-> 42 87-> 43 100->
[49] 52-> 44 21-> 45 54-> 46 32-> 49 92-> 49 6-> 50 17-> 50 13->
+ ... omitted several edges
```

Adjusted graph will be outputted, with updated "pagerank" and "name" as vertex attributes.

Please note `diff_graph()`, `multiplex_page_rank()`, `clean_graph()` and `adjust_graph()` can be used in combination for customized PageRank analysis tasks.

3 Prioritizing TFs in GRNs

3.1 Generating GRNs from Multi-Omics Profiles

The `aracne_network()` can re-format ARACNe network in regulon object for PageRank analysis. It can also handle GRNs reverse engineered using other algorithms, as long as such

GRNs are written in regulon object.

```
> library(bcellViper)
> data(bcellViper)
> head(aracne_network(regulon[1:10]))
```

	reg	target	direction
1	AATF	SAMM50	1
2	AATF	DRG1	1
3	AATF	ATIC	1
4	AATF	SMARCC1	1
5	AATF	AHCY	1
6	AATF	HSD17B10	1

The `accessibility_network()` can build network from accessibility, e.g. ATAC-Seq peaks.

```
> table <- data.frame(Chr=c("chr1", "chr1"), Start=c(713689, 856337), End=
+                      row.names=c("A", "B"), stringsAsFactors=FALSE)
> regulators=c("FOXF2", "MZF1")
> #peaks and regulators to be analyzed
>
> library(GenomicRanges)
> library(GenomicFeatures)
> library(TxDb.Hsapiens.UCSC.hg19.knownGene)
> library(org.Hs.eg.db)
> library(annotate)
> promoter <- promoters(genes(TxDb.Hsapiens.UCSC.hg19.knownGene))
> names(promoter) <- getSYMBOL(names(promoter), data="org.Hs.eg")
> promoter <- promoter[!is.na(names(promoter))]
> #get promoter regions
>
> library(JASPAR2018)
> library(TFBSTools)
> library(motifmatchr)
> pfm <- getMatrixSet(JASPAR2018, list(species="Homo sapiens"))
> pfm <- pfm[unlist(lapply(pfm, function(x) name(x))) %in% regulators]
> #get regulator position frequency matrix (PFM) list
>
> library(BSgenome.Hsapiens.UCSC.hg19)
> accessibility_network(table, promoter, pfm, "BSgenome.Hsapiens.UCSC.hg19")

      target    reg
1 LOC100288069 FOXF2
```

```

2 LOC100288069 MZF1
3     LINC02593 FOXF2
4         SAMD11 FOXF2
5     LINC02593 MZF1
6         SAMD11 MZF1

```

The `conformation_network()` can build network from conformation, e.g. HiChIP records.

```

> table <- data.frame(Chr1=c("chr1", "chr1"), Position1=c(569265, 713603),
+                     Chr2=c("chr4", "chr1"), Position2=c(206628, 715110),
+                     row.names=c("A", "B"), stringsAsFactors=FALSE)
> regulators=c("FOXF2", "MZF1")
> #peaks and regulators to be analyzed
>
> promoter <- promoters(genes(TxDb.Hsapiens.UCSC.hg19.knownGene))
> names(promoter) <- getSYMBOL(names(promoter), data="org.Hs.eg")
> promoter <- promoter[!is.na(names(promoter))]
> #get promoter regions
>
> pfm <- getMatrixSet(JASPAR2018, list(species="Homo sapiens"))
> pfm <- pfm[unlist(lapply(pfm, function(x) name(x))) %in% regulators]
> #get regulator position frequency matrix (PFM) list
>
> conformation_network(table, promoter, pfm, "BSgenome.Hsapiens.UCSC.hg19",

      target    reg
1      ZNF876P MZF1
2 LOC100288069 FOXF2
3 LOC100288069 MZF1

```

3.2 Filter GRNs with Expression Profiles

The `P_graph()` can filter GRNs by quantifying joint and margin probability distributions of regulator-target pairs. Statistically significant non-random regulator-target pairs will be kept.

```

> dset <- exprs(dset)
> net <- do.call(rbind, lapply(1:10, function(i, regulon){
+   data.frame(reg=rep(names(regulon)[i], 10),
+             target=names(regulon[[i]][[1]])[1:10],
+             stringsAsFactors = FALSE)}, regulon=regulon))
> P_graph(dset, net, method="difference", null=NULL, threshold=0.05)

```

[illegible]

[illegible]

This image shows a full page of primary-ruled paper. It features multiple sets of horizontal dashed lines for writing, each set bounded by two vertical solid lines that serve as margins. The margins are wider on the left side than on the right. There are 10 such sets of ruled lines across the page, providing ample space for handwriting practice.

[illegible]

[illegible]

[illegible]


```

|
|=====
|
|=====
|
|=====
|
|=====
|
|=====
|
|=====
|
+ attr: name (v/c), pagerank (v/n), pvalue (e/n)
+ edges from ffbb61f (vertex names):
[1] PPM1G ->AATF    CTBP2 ->APP    TAGLN ->APP    MTSS1 ->APP    JMJD1C->AR

```

3.3 Session Information

```

> sessionInfo()

R Under development (unstable) (2025-03-02 r87868)
Platform: aarch64-apple-darwin20
Running under: macOS Ventura 13.7.1

Matrix products: default
BLAS:   /Library/Frameworks/R.framework/Versions/4.5-arm64/Resources/lib/libcblas.dylib
LAPACK: /Library/Frameworks/R.framework/Versions/4.5-arm64/Resources/lib/liblapack.dylib

locale:
[1] C/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8

time zone: America/New_York
tzcode source: internal

attached base packages:
[1] stats4      stats      graphics  grDevices  utils      datasets  methods
[8] base

other attached packages:
[1] BSgenome.Hsapiens.UCSC.hg19_1.4.3
[2] BSgenome_1.75.1
[3] rtracklayer_1.67.1
[4] BiocIO_1.17.1

```

- [5] Biostrings_2.75.4
- [6] XVector_0.47.2
- [7] motifmatchr_1.29.0
- [8] TFBSTools_1.45.2
- [9] JASPAR2018_1.1.1
- [10] annotate_1.85.0
- [11] XML_3.99-0.18
- [12] org.Hs.eg.db_3.21.0
- [13] TxDb.Hsapiens.UCSC.hg19.knownGene_3.2.2
- [14] GenomicFeatures_1.59.1
- [15] AnnotationDbi_1.69.0
- [16] GenomicRanges_1.59.1
- [17] GenomeInfoDb_1.43.4
- [18] IRanges_2.41.3
- [19] S4Vectors_0.45.4
- [20] bcellViper_1.43.0
- [21] Biobase_2.67.0
- [22] BiocGenerics_0.53.6
- [23] generics_0.1.3
- [24] pageRank_1.17.0

loaded via a namespace (and not attached):

- [1] KEGGREST_1.47.0 DirichletMultinomial_1.49.0
- [3] SummarizedExperiment_1.37.0 rjson_0.2.23
- [5] caTools_1.18.3 lattice_0.22-6
- [7] vctrs_0.6.5 tools_4.5.0
- [9] bitops_1.0-9 curl_6.2.1
- [11] parallel_4.5.0 RSQLite_2.3.9
- [13] blob_1.2.4 pkgconfig_2.0.3
- [15] Matrix_1.7-3 lifecycle_1.0.4
- [17] GenomeInfoDbData_1.2.14 compiler_4.5.0
- [19] Rsamtools_2.23.1 codetools_0.2-20
- [21] RCurl_1.98-1.16 yaml_2.3.10
- [23] crayon_1.5.3 BiocParallel_1.41.2
- [25] DelayedArray_0.33.6 cachem_1.1.0
- [27] abind_1.4-8 gtools_3.9.5
- [29] restfulr_0.0.15 fastmap_1.2.0
- [31] grid_4.5.0 cli_3.6.4
- [33] SparseArray_1.7.6 magrittr_2.0.3
- [35] S4Arrays_1.7.3 TFMPvalue_0.0.9
- [37] UCSC.utils_1.3.1 bit64_4.6.0-1
- [39] pwalign_1.3.2 httr_1.4.7

[41]	matrixStats_1.5.0	igraph_2.1.4
[43]	bit_4.6.0	png_0.1-8
[45]	memoise_2.0.1	rlang_1.1.5
[47]	Rcpp_1.0.14	xtable_1.8-4
[49]	glue_1.8.0	DBI_1.2.3
[51]	seqLogo_1.73.0	jsonlite_1.9.1
[53]	R6_2.6.1	MatrixGenerics_1.19.1
[55]	GenomicAlignments_1.43.0	

4 References

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3. Brin, Sergey, and Lawrence Page. "The anatomy of a large-scale hypertextual web search engine." (1998).
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