destiny

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October 14, 2015

Introduction

Diffusion maps are spectral method for non-linear dimension reduction introduced by Coifman et al. (2005). Diffusion maps are based on a distance metric (diffusion distance) which is conceptually relevant to how differentiating cells follow noisy diffusion-like dynamics, moving from a pluripotent state towards more differentiated states.

The R package destiny implements the formulation of diffusion maps presented in Haghverdi et al. (2015) which is especially suited for analyzing single-cell gene expression data from time-course experiments. It implicitly arranges cells along their developmental path, with bifurcations where differentiation events occur.

In particular we follow Haghverdi et al. (2015) and present an implementation of diffusion maps in R that is less affected by sampling density heterogeneities and thus capable of identifying both abundant and rare cell populations. In addition, destiny implements complex noise models reflecting zero-inflation/censoring due to drop-out events in single-cell qPCR data and allows for missing values. Finally, we further improve on the implementation from Haghverdi et al. (2015), and implement a nearest neighbour approximation capable of handling very large data sets of up to 300.000 cells.

For those familiar with R, and data preprocessing, we recommend the section Plotting.

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1 Preprocessing of single qPCR data

As an example, we present in the following the preprocessing of data from Guo et al. (2010). This dataset was produced by the Biomark RT-qPCR system and contains Ct values for 48 genes of 442 mouse embryonic stem cells at 7 different developmental time points, from the zygote to blastocyst.

Starting at the totipotent 1-cell stage, cells transition smoothly in the transcriptional landscape towards either the trophoectoderm lineage or the inner cell mass. Subsequently, cells transition from the inner cell mass either towards the endoderm or epiblast lineage. This smooth transition from one developmental state to another, including two bifurcation events, is reflected in the expression profiles of the cells and can be visualized using destiny.

Import

Downloading the table S4 from the publication website will give you a spreadsheet "mmc4.xls", from which the data can be loaded:

```
In [2]: library(xlsx)
    raw.ct <- read.xlsx('mmc4.xls', sheetName = 'Sheet1')
    raw.ct[1:9, 1:9] #preview of a few rows and columns</pre>
```

Out[2]:		Cell	Actb	Ahcy	Aqp3	Atp12a	Bmp4	Cdx2	Creb312	Cebpa
	1	1C 1	14.01	19.28	23.89	28	28	21.28	20.84	28
	2	1C 2	13.68	18.56	28	28	28	23.43	20.93	28
	3	1C 3	13.42	18.19	26.18	28	28	22.87	19.61	28
	4	1C 4	13.69	18.59	28	28	28	23.28	20.72	28
	5	1C 5	13.47	18.6	24.2	28	28	24.19	21.75	23.69
	6	1C 6	12.86	17.37	25.53	28	28	21.87	21.27	28
	7	1C 7	12.95	17.37	23.93	28	28	22.74	21.12	28
	8	1C 8	12.77	18.4	23.68	28	28	24.14	19.8	28
	9	1C 9	13.29	18.26	28	28	28	21.91	21.18	28

The value 28 is the assumed background expression of 28 cycle times.

In order to easily clean and normalize the data without mangling the annotations, we convert the data.frame into a Bioconductor ExpressionSet using the as.ExpressionSet function from the destiny package, and assign it to the name ct:

In [3]: library(destiny)

```
ct <- as.ExpressionSet(raw.ct)
ct
Out[3]: ExpressionSet (storageMode: lockedEnvironment)
assayData: 48 features, 442 samples
    element names: exprs
protocolData: none
phenoData
    sampleNames: 1 2 ... 442 (442 total)
    varLabels: Cell
    varMetadata: labelDescription
    featureData: none
    experimentData: use 'experimentData(object)'
    Annotation:</pre>
```

The advantage of ExpressionSet over data.frame is that tasks like normalizing the expressions are both faster and do not accidentally destroy annotations by applying "normalization" to columns that are not expressions. The approach of handling a separate expression matrix and annotation data.frame requires you to be careful when adding or removing samples on both variables, while ExpressionSet does it internally for you.

The object internally stores an expression matrix of features \times samples, retrievable using exprs(ct), and an annotation data.frame of samples \times annotations as phenoData(ct). Note that the expression matrix is transposed compared to the usual samples \times features data.frame.

Data cleaning

We remove all cells that have a value bigger than the background expression, indicating data points not available (NA). Also we remove cells from the 1 cell stage embryos, since they were treated systematically different (Guo et al. (2010)).

For this, we add an annotation column containing the embryonic cell stage for each sample by extracting the number of cells from the "Cell" annotation column:

We then use the new annotation column to create two filters:

```
In [5]: # cells from 2+ cell embryos
    have.duplications <- phenoData(ct)$num.cells > 1
    # cells with values ≤ 28
    normal.vals <- apply(exprs(ct), 2, function(sample) all(sample <= 28))</pre>
```

We can use the combination of both filters to exclude both non-divided cells and such containing Ct values higher than the baseline, and store the result as cleaned.ct:

In [6]: cleaned.ct <- ct[, have.duplications & normal.vals]</pre>

Normalization

Finally we follow Guo et al. (2010) and normalize each cell using the endogenous controls Actb and Gapdh by subtracting their average expression for each cell. Note that it is not clear how to normalise sc-qPCR data as the expression of housekeeping genes is also stochastic. Consequently, if such housekeeping normalisation is performed. It is crucial to take the mean of several genes.

```
In [7]: housekeepers <- c('Actb', 'Gapdh') # houskeeper gene names</pre>
```

```
normalizations <- colMeans(exprs(cleaned.ct)[housekeepers, ])</pre>
```

```
normalized.ct <- cleaned.ct
exprs(normalized.ct) <- exprs(normalized.ct) - normalizations</pre>
```

The resulting ExpressionSet contains the normalized Ct values of all cells retained after cleaning.

2 Plotting

The data necessary to create a diffusion map with our package is a a cell×gene matrix or data.frame, or alternatively an ExpressionSet (which has a gene×cell exprs matrix). In order to create a DiffusionMap object, you just need to supply one of those formats as first parameter to the DiffusionMap function. In the case of a data.frame, each floating point column is interpreted as expression levels, and columns of different type (e.g. factor, character or integer) are assumed to be annotations and ignored. Note that single-cell RNA-seq count data should be transformed using a variance-stabilizing transformation (e.g. log or rlog); the Ct scale for qPCR data is logarithmic already (an increase in 1 Ct corresponds to a doubling of transcripts).

In order to create a diffusion map to plot, you have to call DiffusionMap, optionally with parameters. If the number of cells is small enough (< ~1000), you do not need to specify approximations like k (for k nearest neighbors):

Simply calling plot on the resulting object dif will visualize the diffusion components:

In [9]: plot(dif)



DC1

The diffusion map nicely illustrates a branching during the first days of embryonic development.

The annotation column containing the cell stage can be used to annotate our diffusion map. Using the annotation as col parameter will automatically color the map using the current palette().



Three branches appear in the map, with a bifurcation occurring the 16 cell stage and the 32 cell stage. The diffusion map is able to arrange cells according to their expression profile: Cells that divided the most and the least appear at the tips of the different branches.

In order to display a 2D plot we supply a vector containing two diffusion component numbers (here 1 & 2) as second argument.



Alternative visualizations

Diffusion maps consist of eigenvectors called Diffusion Components (DCs) and corresponding eigenvalues. Per default, the first 20 are returned.

You are also able to use packages for interative plots like rgl in a similar fashion, by directly subsetting the DCs using eigenvectors(dif):

For the popular ggplot2 package, there is built in support in the form of a fortify.DiffusionMap method, which allows to use DiffusionMap objects as data parameter in the ggplot and qplot functions:

```
In [13]: library(ggplot2)
    qplot(DC1, DC2, data = dif, colour = factor(num.cells)) +
        scale_color_brewer(palette = 'Spectral')
    # or alternatively:
    #ggplot(dif, aes(DC1, DC2, colour = factor(num.cells))) + ...
```



As aesthetics, all diffusion components, gene expressions, and annotations are available. If you plan to make many plots, create a data.frame first by using as.data.frame(dif) or fortify(dif), assign it to a variable name, and use it for plotting.

3 Parameter selection

Two important parameters to DiffusionMap, dims and sigma, crucially determine the diffusion map approximation and are explained in detail in the following section.

Other parameters are explained at the end of this section.

Dimensions dims

Diffusion maps consist of the eigenvectors (which we refer to as diffusion components) and corresponding eigenvalues of the diffusion distance matrix. The latter indicate the diffusion components' importance, i.e. how well the eigenvectors approximate the data. The eigenvectors are decreasingly meaningful.



Here, the first four apparently provide the best approximation. The later DCs often become noisy and less useful: In [16]: par(mfrow = c(1, 2), mar = c(2,2,2,2))

plot(dif, 3:4, pch = 20, col.by = 'num.cells', draw.legend = FALSE)
plot(dif, 19:20, pch = 20, col.by = 'num.cells', draw.legend = FALSE)



Gaussian kernel width sigma

The other important parameter for DiffusionMap is the Gaussian kernel width sigma (σ) that determines the transition probability between data points. The default call of destiny – DiffusionMap(data) – automatically estimates sigma using a heuristic. It is also possible to specify this parameter manually to tweak the result. The eigenvector plot explained above will show a continuous decline instead of sharp drops if either the dataset is too big or the sigma is chosen too small.

The sigma estimation algorithm is explained in detail in Haghverdi et al. (2015). In brief, it works by finding a maximum in the slope of the log-log plot of local density versus sigma. Using find.sigmas

An efficient variant of that procedure is provided by find.sigma. This function determines the optimal sigma for a subset of the given data and provides the default sigma for a DiffusionMap call. Due to a different starting point, the resulting sigma is different from above:

Out[18]: 10.8945955274194

The resulting diffusion map's approximation depends on the chosen sigma. Note that the sigma estimation heuristic only finds local optima and even the global optimum of the heuristic might not be ideal for your data.

```
In [19]: par(pch = 20, mfrow = c(2, 2), mar = c(3,2,2,2))
          for (sigma in c(2, 5, optimal.sigma(sigmas), 100))
               plot(DiffusionMap(normalized.ct, sigma), 1:2,
                     main = substitute(sigma == s, list(s = round(sigma,2))),
                     col.by = 'num.cells', draw.legend = FALSE)
                              \sigma = 2
                                                          \sigma = 5
                  DC2
                                              DC2
                               DC1
                                                           DC1
                             σ = 10.89
                                                          \sigma = 100
                  DC2
                                              DC2
                                                           DC1
                               DC1
```

Other parameters

If the automatic exclusion of categorical and integral features for data frames is not enough, you can also supply a vector of variable names or indices to use with the vars parameter. If you find that calculation time or used memory is too large, the parameter k allows you to decrease the quality/runtime+memory ratio by limiting the number of transitions calculated and stored. It is typically not needed if you have less than few thousand cells. The n.eigs parameter specifies the number of diffusion components returned.

For more information, consult help(DiffusionMap).

4 Missing and uncertain values

destiny is particularly well suited for gene expression data due to its ability to cope with missing and uncertain data.

Censored values

Platforms such as RT-qPCR cannot detect expression values below a certain threshold. To cope with this, destiny allows to censor specific values. In the case of Guo et al. (2010), only up to 28 qPCR cycles were counted. All transcripts that would need more than 28 cycles are grouped together under this value. This is illustrated by gene Aqp3:



Histogram of Aqp3 Ct

For our censoring noise model we need to identify the limit of detection (LoD). While most researchers use a global LoD of 28, reflecting the overall sensitivity of the qPCR machine, different strategies to quantitatively establish this gene-dependent LoD exist. For example, dilution series of bulk data can be used to establish an LoD such that a qPCR reaction will be detected with a specified probability if the Ct value is below the LoD. Here, we use such dilution series provided by Guo et al. and first determine a gene-wise LoD as the largest Ct value smaller than 28. We then follow the manual Application Guidance: Single-Cell Data Analysis of the popular Biomarks system and determine a global LoD as the median over the gene-wise LoDs. We use the dilution series from table S7 (mmc6.xls). If you have problems with the speed of read.xlsx, consider storing your data in tab separated value format and using read.delimor read.ExpressionSet.

lods <- apply(dilutions, 2, function(col) col[[max(which(col != 28))]])</pre>

lod <- ceiling(median(lods))
lod</pre>

Out[21]: 25

This LoD of 25 and the maximum number of cycles the platform can perform (40), defines the uncertainty range that denotes the possible range of censored values in the censoring model. Using the mean of the normalization vector, we can adjust the uncertainty range and censoring value to be more similar to the other values in order to improve distance measures between data points:

```
In [22]: lod.norm <- ceiling(median(lods) - mean(normalizations))
    max.cycles.norm <- ceiling(40 - mean(normalizations))
    list(lod.norm = lod.norm, max.cycles.norm = max.cycles.norm)</pre>
```

Out[22]: \$lod.norm 10 \$max.cycles.norm 25

We then also need to set the normalized values that should be censored – namely all data points were no expression was detected after the LoD – to this special value, because the values at the cycle threshold were changed due to normalization.

Now we call the the DiffusionMap function using the censoring model:



Compared to the diffusion map created without censoring model, this map looks more homogeneous since it contains more data points.

Missing values

Gene expression experiments may fail to produce some data points, conventionally denoted as "not available" (NA). By calling DiffusionMap(..., missings = c(total.minimum, total.maximum)), you can specify the parameters for the missing value model.

As in the data from Guo et al. (2010) no missing values occurred, we illustrate the capacity of destiny to handle missing values by artificially treating ct values of 999 (i. e. data points were no expression was detected after 40 cycles) as missing. This is purely for illustrative purposes and in practice these values should be treated as censored as illustrated in the previous section.

```
In [25]: # remove rows with divisionless cells
    ct.w.missing <- ct[, phenoData(ct)$num.cells > 1L]
    # and replace values larger than the baseline
    exprs(ct.w.missing)[exprs(ct.w.missing) > 28] <- NA</pre>
```

We then perform normalization on this version of the data:

w.missing <- ct.w.missing
exprs(w.missing) <- exprs(w.missing) - housekeep</pre>

exprs(w.missing)[is.na(exprs(ct.w.missing))] <- lod.norm</pre>

Finally, we create a diffusion map with both missing value model and the censoring model from before:



This result looks very similar to our previous diffusion map since only six additional data points have been added. However if your platform creates more missing values, including missing values will be more useful.

5 Prediction

In order to project cells into an existing diffusion map, for example to compare two experiments measured by the same platform or to add new data to an existing map, we implemented dm.predict. It calculates the transition probabilities between datapoints in old and new data and projects cells into the diffusion map using the existing diffusion components.

As an example we assume that we created a diffusion map from one experiment on 64 cell stage embryos:

```
In [28]: ct64 <- censored.ct[, phenoData(censored.ct)$num.cells == 64]</pre>
```

dif64 <- DiffusionMap(ct64)</pre>

Let us compare the expressions from the 32 cell state embryos to the existing map. We use dm.predict to create the diffusion components for the new cells using the existing diffusion components from the old data:

By providing the more and col.more parameters of the plot function, we show the first two DCs for both old and new data:



Clearly, the 32 and 64 cell state embryos occupy similar regions in the map, while the cells from the 64 cell state are developed further.

6 Troubleshooting

There are several properties of data that can yield subpar results. This section explains a few strategies of dealing with them:

read.xlsx is slow: Using read.xlsx2 and manually converting the text columns into numbers aftwerwards could be a solution, but using tab separated values (TSV) or comma separated values (CSV) is more portable and robust than Microsoft Excel.

Preprocessing: if there is a strong dependency of the variance on the mean in your data (as for scRNA-Seq count data), use a variance stabilizing transformation such as the square root or a (regularized) logarithm before running *destiny*.

Outliers: If a Diffusion Component strongly separates some outliers from the remaining cells such that there is a much greater distance between them than within the rest of the cells (i. e. almost two discrete values), consider removing those outliers and recalculating the map, or simply select different Diffusion Components. It may also a be a good idea to check whether the outliers are also present in a PCA plot to make sure they are not biologically relevant.

Large datasets: If memory is not sufficient and no machine with more RAM is available, the k parameter could be decreased. In addition (particularly for >500,000 cells), you can also downsample the data (possibly in a density dependent fashion).

"Large-p-small-n" data: E.g. for scRNA-Seq, it is may be necessary to first perform a Principal Component Analysis (PCA) on the data (e.g. using prcomp or princomp) and to calculate the Diffusion Components from the Principal Components (typically using the top 50 components yields good results).

References

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