

# Package ‘GraphAlignment’

October 8, 2014

**Version** 1.28.0

**Date** 2013-01-15

**Title** GraphAlignment

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**Description** Graph alignment is an extension package for the R programming environment which provides functions for finding an alignment between two networks based on link and node similarity scores. (J. Berg and M. Laessig, "Cross-species analysis of biological networks by Bayesian alignment", PNAS 103 (29), 10967-10972 (2006))

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**URL** <http://www.thp.uni-koeln.de/~berg/GraphAlignment/>

**biocViews** GraphAndNetwork, Network

## R topics documented:

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AlignedPairs	<i>Get aligned node pairs</i>
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### Description

Create a matrix of pairs of aligned nodes from networks A and B using the permutation vector P, where P is in the format returned by `AlignNetworks()`.

### Usage

```
AlignedPairs(A, B, P)
```

### Arguments

A	adjacency matrix for network A
B	adjacency matrix for network B
P	permutation vector to be used as the alignment

### Details

This function creates a matrix containing pairs of aligned nodes from networks A and B using the permutation vector P, where P is in the format returned by [AlignNetworks](#).

### Value

The return value is a matrix with two columns. The number of rows is equal to the number of aligned node pairs. Each row in the matrix denotes a pair of aligned nodes. In each row, the first element (index 1) is the label of a node in network A, and the second element (index 2) is the label of a node in network B.

### Author(s)

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**Examples**

```

ex<-GenerateExample(dimA=22, dimB=22, filling=.5, covariance=.6,
  symmetric=TRUE, numOrths=10, correlated=seq(1,18))

pinitial<-InitialAlignment(psize=34, r=ex$r, mode="reciprocal")

lookupLink<-seq(-2,2,.5)
linkParams<-ComputeLinkParameters(ex$a, ex$b, pinitial, lookupLink)

lookupNode<-c(-.5, .5, 1.5)
nodeParams<-ComputeNodeParameters(dimA=22, dimB=22, ex$r,
  pinitial, lookupNode)

al<-AlignNetworks(A=ex$a, B=ex$b, R=ex$r, P=pinitial,
  linkScore=linkParams$l,
  selfLinkScore=linkParams$ls,
  nodeScore1=nodeParams$s1, nodeScore0=nodeParams$s0,
  lookupLink=lookupLink, lookupNode=lookupNode,
  bStart=.1, bEnd=30,
  maxNumSteps=50)

alignedPairs<-AlignedPairs(A=ex$a, B=ex$b, al)

```

AlignNetworks

*Align networks***Description**

Align networks A and B.

**Usage**

```
AlignNetworks(A, B, R, P, linkScore, selfLinkScore, nodeScore1,
  nodeScore0, lookupLink, lookupNode, bStart, bEnd, maxNumSteps, clamp=TRUE,
  directed=FALSE)
```

**Arguments**

A	adjacency matrix for network A
B	adjacency matrix for network B
R	node similarity matrix
P	permutation vector to be used as the initial alignment (see <a href="#">InitialAlignment</a> )
linkScore	link score matrix (see <a href="#">ComputeLinkParameters</a> )
selfLinkScore	self link score matrix (see <a href="#">ComputeLinkParameters</a> )
nodeScore1	node score vector (s1) (see <a href="#">ComputeNodeParameters</a> )
nodeScore0	node score vector for unaligned nodes (s0) (see <a href="#">ComputeNodeParameters</a> )

lookupLink	link bin lookup table (see <a href="#">GetBinNumber</a> )
lookupNode	node bin lookup table (see <a href="#">GetBinNumber</a> )
bStart	start scaling value for simulated annealing
bEnd	end scaling value for simulated annealing
maxNumSteps	maximum number of steps
clamp	clamp values to range when performing bin lookups
directed	whether input networks should be treated as directed graphs

### Details

This function finds an alignment between the two input networks, specified in the form of adjacency matrices, by repeatedly calling [ComputeM](#) and [LinearAssignment](#), up to maxNumSteps times. Simulated annealing is performed if a range is specified in the bStart and bEnd arguments. This simple procedure is described in detail in [Berg, Laessig 2006]. Different procedures can easily be implemented by the user.

In each step, the matrix M is calculated from the scoring parameters and the current permutation vector P. The result is then normalized to the range [-1, 1] and, if simulated annealing is enabled, a random matrix depending on the current simulated annealing parameters is added. The linear assignment routine is used to calculate the value of P which is used to compute M in the next step.

If the flag directed is set, directed binary networks are encoded by suitable symmetric matrices using [EncodeDirectedGraph](#). The corresponding 3x3 matrices of the link score are computed from the 2x2 matrices given as input.

Simulated annealing is enabled if bStart differs from bEnd. In this case, a value  $bStep = bEnd - bStart / (maxNumSteps - 1)$  is calculated. In step n, the random matrix which is added to M is scaled by the factor  $1 / [bStart + (n - 1) * bStep]$ .

### Value

The return value is a permutation vector p which aligns nodes from network a with nodes from network B (including dummy nodes). The returned permutation should be read in the following way: the node i in the network A is aligned to that node in the network B which label is at the i-th position of the permutation vector p. If the label at this position is larger than the size of the network B, the node i is not aligned.

### Author(s)

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

### References

Berg, J. & Laessig, M. (2006) Proc. Natl. Acad. Sci. USA 103, 10967-10972.

**Examples**

```

ex<-GenerateExample(dimA=22, dimB=22, filling=.5, covariance=.6,
  symmetric=TRUE, numOrths=10, correlated=seq(1,18))

pinitial<-InitialAlignment(psize=34, r=ex$r, mode="reciprocal")

lookupLink<-seq(-2,2,.5)
linkParams<-ComputeLinkParameters(ex$a, ex$b, pinitial, lookupLink)

lookupNode<-c(-.5, .5, 1.5)
nodeParams<-ComputeNodeParameters(dimA=22, dimB=22, ex$r,
  pinitial, lookupNode)

al<-AlignNetworks(A=ex$a, B=ex$b, R=ex$r, P=pinitial,
  linkScore=linkParams$l,
  selfLinkScore=linkParams$l,
  nodeScore1=nodeParams$s1, nodeScore0=nodeParams$s0,
  lookupLink=lookupLink, lookupNode=lookupNode,
  bStart=.1, bEnd=30,
  maxNumSteps=50)

```

AnalyzeAlignment

*Analyze an alignment***Description**

Analyze an alignment between two networks.

**Usage**

```
AnalyzeAlignment(A, B, R, P, lookupNode, epsilon, clamp)
```

**Arguments**

A	adjacency matrix for network A
B	adjacency matrix for network B
R	node similarity matrix
P	permutation vector
lookupNode	node bin lookup vector
epsilon	node similarity threshold
clamp	clamp values to range when performing bin lookups

**Details**

This function analyzes an alignment and returns various characteristics.

**Value**

The return value is a list containing the results. Defined values are:

na - number of aligned node pairs

nb - number of aligned node pairs where neither partner has appreciable sequence similarity with any node in the other network. Appreciable sequence similarity means that  $r > \epsilon$ . Formally, this is the number of aligned node pairs (ia, ib), where no jb exists such that  $R[ia, jb] > \epsilon$  and no ja such that  $R[ja, ib] > \epsilon$ .

nc - number of aligned node pairs, where the partners have no appreciable sequence similarity, but one or both of them has appreciable sequence similarity with some other node in the other network. Formally, this is the number of aligned node pairs (ia, ib) with  $R[ia, ib] < \epsilon$  but jb or ja exists, such that  $R[ia, jb] > \epsilon$  or  $R[ja, ib] > \epsilon$ .

**Author(s)**

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**Examples**

```
ex<-GenerateExample(dimA=22, dimB=22, filling=.5, covariance=.6,
  symmetric=TRUE, numOrths=10, correlated=seq(1,18))

pinitial<-InitialAlignment(psize=34, r=ex$r, mode="reciprocal")

lookupLink<-seq(-2,2,.5)
linkParams<-ComputeLinkParameters(ex$a, ex$b, pinitial, lookupLink)

lookupNode<-c(-.5, .5,1.5)
nodeParams<-ComputeNodeParameters(dimA=22, dimB=22, ex$r,
  pinitial, lookupNode)

al<-AlignNetworks(A=ex$a, B=ex$b, R=ex$r, P=pinitial,
  linkScore=linkParams$linkScore,
  selfLinkScore=linkParams$selfLinkScore,
  nodeScore1=nodeParams$nodeScore1, nodeScore0=nodeParams$nodeScore0,
  lookupLink=lookupLink, lookupNode=lookupNode,
  bStart=.1, bEnd=30,
  maxNumSteps=50)

AnalyzeAlignment(A=ex$a, B=ex$b, R=ex$r, P=al, lookupNode,
  epsilon=.5)
```

---

ComputeLinkParameters *Compute link parameters*

---

**Description**

Compute the optimal scoring parameters (link score) for a given alignment.

**Usage**

```
ComputeLinkParameters(A, B, P, lookupLink, clamp=TRUE)
```

**Arguments**

A	adjacency matrix for network A
B	adjacency matrix for network B
P	permutation vector (see <a href="#">InitialAlignment</a> , <a href="#">AlignNetworks</a> )
lookupLink	link bin lookup table (see <a href="#">GetBinNumber</a> )
clamp	clamp values to range when performing bin lookups

**Details**

This function computes optimal link score parameters for use with [ComputeM](#) and [AlignNetworks](#). It takes two matrices as well as an initial alignment P and the lookup table for link binning, lookupLink, as parameters.

**Value**

The return value is a list containing the self link score matrix (lsSelf) and the link score matrix (ls).

**Author(s)**

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**Examples**

```
ex<-GenerateExample(dimA=22, dimB=22, filling=.5, covariance=.6,
  symmetric=TRUE, numOrths=10, correlated=seq(1,18))

pinitial<-InitialAlignment(psize=34, r=ex$r, mode="reciprocal")

lookupLink<-seq(-2,2,.5)
linkParams<-ComputeLinkParameters(ex$a, ex$b, pinitial, lookupLink)
```

---

ComputeM

*Compute score matrix M*

---

**Description**

Compute the score matrix M.

**Usage**

```
ComputeM(A, B, R, P, linkScore, selfLinkScore, nodeScore1,
  nodeScore0, lookupLink, lookupNode, clamp=TRUE)
```

**Arguments**

A	adjacency matrix for network A
B	adjacency matrix for network B
R	node similarity matrix
P	permutation vector to be used as the initial alignment (see <a href="#">InitialAlignment</a> )
linkScore	link score matrix (see <a href="#">ComputeLinkParameters</a> )
selfLinkScore	self link score matrix (see <a href="#">ComputeLinkParameters</a> )
nodeScore1	node score vector (s1) (see <a href="#">ComputeNodeParameters</a> )
nodeScore0	node score vector for unaligned nodes (s0) (see <a href="#">ComputeNodeParameters</a> )
lookupLink	link bin lookup table (see <a href="#">GetBinNumber</a> )
lookupNode	node bin lookup table (see <a href="#">GetBinNumber</a> )
clamp	clamp values to range when performing bin lookups

**Details**

This function computes the score Matrix M from the network adjacency matrices A and B, the node similarity matrix R, an alignment P (given as a permutation vector) and the node and link scores with their associated binning information. The alignment P is either generated by the previous iterative step, or, initially, by using [InitialAlignment](#). The matrix M is then given to the linear assignment solver to compute the new alignment.

**Value**

The return value is the score matrix M.

**Author(s)**

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**Examples**

```
ex<-GenerateExample(dimA=22, dimB=22, filling=.5, covariance=.6,
  symmetric=TRUE, numOrths=10, correlated=seq(1,18))

pinitial<-InitialAlignment(psize=34, r=ex$r, mode="reciprocal")

lookupLink<-seq(-2,2,.5)
linkParams<-ComputeLinkParameters(ex$a, ex$b, pinitial, lookupLink)

lookupNode<-c(-.5,.5,1.5)
nodeParams<-ComputeNodeParameters(dimA=22, dimB=22, ex$r,
  pinitial, lookupNode)

ComputeM(A=ex$a, B=ex$b, R=ex$r, P=pinitial,
  linkScore=linkParams$linkScore,
  selfLinkScore=linkParams$selfLinkScore,
  nodeScore1=nodeParams$nodeScore1, nodeScore0=nodeParams$nodeScore0,
  lookupLink=lookupLink, lookupNode=lookupNode)
```



---

ComputeNodeParameters *Compute node parameters*

---

## Description

Compute the optimal scoring parameters (node score) for a given alignment.

## Usage

```
ComputeNodeParameters(dimA, dimB, R, P, lookupNode, clamp=TRUE)
```

## Arguments

dimA	size of network A
dimB	size of network B
R	node similarity score matrix
P	permutation vector (see <a href="#">InitialAlignment</a> , <a href="#">AlignNetworks</a> )
lookupNode	node bin lookup table (see <a href="#">GetBinNumber</a> )
clamp	clamp values to range when performing bin lookups

## Details

This function computes optimal node score parameters for use with [ComputeM](#) and [AlignNetworks](#). It takes the size of the networks, a matrix of node similarities R, an initial alignment P, and the lookup table for node binning, lookupNode, as parameters.

## Value

The return value is list containing the node score vectors s0 and s1.

## Author(s)

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

## Examples

```
ex<-GenerateExample(dimA=22, dimB=22, filling=.5, covariance=.6,
  symmetric=TRUE, numOrths=10, correlated=seq(1,18))

pinitial<-InitialAlignment(psize=34, r=ex$r, mode="reciprocal")

lookupNode<-c(-.5, .5, 1.5)
nodeParams<-ComputeNodeParameters(dimA=22, dimB=22, ex$r,
  pinitial, lookupNode)
```

---

ComputeScores	<i>Compute scores</i>
---------------	-----------------------

---

**Description**

Compute scores.

**Usage**

```
ComputeScores(A, B, R, P, linkScore, selfLinkScore, nodeScore1,  
             nodeScore0, lookupLink, lookupNode, symmetric=TRUE, clamp=TRUE)
```

**Arguments**

A	adjacency matrix for network A
B	adjacency matrix for network B
R	node similarity matrix
P	permutation vector to be used as the initial alignment (see <a href="#">InitialAlignment</a> )
linkScore	link score matrix (see <a href="#">ComputeLinkParameters</a> )
selfLinkScore	self link score matrix (see <a href="#">ComputeLinkParameters</a> )
nodeScore1	node score vector (s1) (see <a href="#">ComputeNodeParameters</a> )
nodeScore0	node score vector for unaligned nodes (s0) (see <a href="#">ComputeNodeParameters</a> )
lookupLink	link bin lookup table (see <a href="#">GetBinNumber</a> )
lookupNode	node bin lookup table (see <a href="#">GetBinNumber</a> )
symmetric	network symmetry flag
clamp	clamp values to range when performing bin lookups

**Details**

This function computes log-likelihood scores for an alignment using the specified scoring tables, two networks A and B and their alignment P. The total score of the alignment has two contributions, the first coming from the sequence homology (node similarity, sn) and the second from the similarity of interaction networks (sl).

**Value**

The return value is a list containing the link score (sl) and the node score (sn).

**Author(s)**

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**Examples**

```

ex<-GenerateExample(dimA=22, dimB=22, filling=.5, covariance=.6,
  symmetric=TRUE, numOrths=10, correlated=seq(1,18))

pinitial<-InitialAlignment(psize=34, r=ex$r, mode="reciprocal")

lookupLink<-seq(-2,2,.5)
linkParams<-ComputeLinkParameters(ex$a, ex$b, pinitial, lookupLink)

lookupNode<-c(-.5, .5, 1.5)
nodeParams<-ComputeNodeParameters(dimA=22, dimB=22, ex$r,
  pinitial, lookupNode)

al<-AlignNetworks(A=ex$a, B=ex$b, R=ex$r, P=pinitial,
  linkScore=linkParams$l,
  selfLinkScore=linkParams$l,
  nodeScore1=nodeParams$s1, nodeScore0=nodeParams$s0,
  lookupLink=lookupLink, lookupNode=lookupNode,
  bStart=.1, bEnd=30,
  maxNumSteps=50)

ComputeScores(A=ex$a, B=ex$b, R=ex$r, P=al,
  linkScore=linkParams$l,
  selfLinkScore=linkParams$l,
  nodeScore1=nodeParams$s1, nodeScore0=nodeParams$s0,
  lookupLink=lookupLink, lookupNode=lookupNode,
  symmetric=TRUE)

```

---

CreateScoreMatrix      *Create score matrix*

---

**Description**

Create a score matrix from two lookup vectors.

**Usage**

```
CreateScoreMatrix(lookupX, lookupY)
```

**Arguments**

lookupX	x lookup vector
lookupY	y lookup vector

**Details**

This function creates a very simple score matrix containing the product of lookup table values for each row and column as its elements. This can be used for testing purposes.

**Value**

The return value is a matrix of link scores.

**Author(s)**

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**Examples**

```
lookupLink <- 0.1*(-10:10)
CreateScoreMatrix(lookupLink, lookupLink)
```

---

EncodeDirectedGraph    *Encode directed graph*

---

**Description**

Encode an adjacency matrix for a directed graph into a symmetric matrix.

**Usage**

```
EncodeDirectedGraph(matrix, P)
```

**Arguments**

matrix	square matrix
P	permutation vector

**Details**

This function encodes an adjacency matrix for a directed graph into a symmetric matrix. Currently only binary directed graphs are implemented. The adjacency matrix of a binary directed graph has elements 0, 1. The same graph can be represented by a symmetric adjacency matrix with elements -1, 0, 1, with the sign of the entry indicating the direction of the link. The result is obtained by setting entries (i, j) and (j, i) of the target matrix  $m'$  to 1 if entry  $m[i, j] = 1$  and  $P[i] > P[j]$  and to -1 if  $m[i, j] = 1$  and  $P[j] > P[i]$ .

**Value**

The return value is a symmetric matrix representing the encoded input matrix.

**Author(s)**

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**Examples**

```
dg <- matrix(c(0, 1, 0, 0, 1, 1, 1, 0, 1), 3, 3)
EncodeDirectedGraph(dg, 1:dim(dg)[1])
```

---

GenerateExample      *Generate example input data*

---

### Description

Generate input data which can be used as an example.

### Usage

```
GenerateExample(dimA, dimB, filling, covariance, symmetric = FALSE,  
numOrths = 0, correlated = NA, distribution = "normal")
```

### Arguments

dimA	size of network A
dimB	size of network B
filling	fraction of entries which are not explicitly set to zero
covariance	covariance of correlated rows and columns
symmetric	generate symmetric matrices
numOrths	number of diagonal elements to set to 1 in example matrix R
correlated	indices of correlated rows and columns
distribution	from which distribution are the values drawn ("normal" or "uniform")

### Details

Symmetric example matrices A, B can be generated by specifying TRUE as the 'symmetric' argument. If the 'numOrths' argument is specified, a number of diagonal elements of R equal to the value will be set to 1. If a vector is specified as the 'correlated' argument, the specified rows and columns will be set to correlated values. Leaving this argument blank will result in pairwise correlations of all entries in A, B (or, if the matrices are of different rank, all elements of the smaller on will be correlated with the corresponding parts of the larger matrix).

### Value

The return value is a list containing example matrices A (a), B (b) and R (r).

### Author(s)

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**Examples**

```

ex <- GenerateExample(dimA = 170, dimB = 140, filling = 0.75,
                     covariance = 0.4, symmetric = TRUE, numOrths = 90,
                     correlated = 1:90, distribution = "normal")

##-- edge weight correlation
image(cor(ex$a[1:140, 1:140], ex$b))
hist(diag(cor(ex$a[1:140, 1:140], ex$b))[1:90])

##-- edge weight distribution
hist(ex$a[ex$a != 0]);
hist(ex$b[ex$b != 0]);

```

---

GetBinNumber

*Get bin number*


---

**Description**

Get the bin number for the argument using the specified lookup vector.

**Usage**

```
GetBinNumber(x, lookup, clamp=TRUE)
```

**Arguments**

x	value to be binned
lookup	lookup vector
clamp	clamp value to lookup range

**Details**

The lookup vector defines the lower and upper boundaries for each bin. The first entry in the lookup vector is the lower boundary of the first bin, while the last value in the lookup vector is the upper boundary of the last bin. For all other entries, entry *i* of the lookup vector defines the upper boundary of the (*i*-1)-th bin and the lower boundary of the *i*-th bin. The number of bins is therefore *n*-1, where *n* is the length of the lookup vector. A lookup vector must have at least two elements.

If clamping is enabled (`clamp=TRUE`), arguments which fall below the lower boundary of the first bin are treated as if they are actually in the first bin. Likewise, values which are above the upper boundary of the last bin are treated as if they are actually in the last bin. If clamping is disabled (`clamp=FALSE`), values outside the lookup range cause an error.

**Value**

This function returns the bin number corresponding to the input value. The bin number is obtained by performing a lookup in the specified lookup vector.

**Author(s)**

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**Examples**

```
lookup <- c(-1, 0, 1)
GetBinNumber(-0.5, lookup)
GetBinNumber(0.5, lookup)
```

---

InitialAlignment	Create initial alignment
------------------	--------------------------

---

**Description**

Create a permutation for an initial alignment. Either "random" or "reciprocal" may be specified as the mode argument.

**Usage**

```
InitialAlignment(psize, r=NA, mode="random")
```

**Arguments**

psize	size of the alignment
r	node similarity score matrix (required for mode 'reciprocal')
mode	type of initial alignment

**Details**

To create a random initial alignment of size psize, the [InitialAlignment](#) function can be used with the mode argument set to "random". If mode is set to "reciprocal", a reciprocal best match algorithm is applied to the input matrix R to find an initial alignment. This mode requires that the psize argument is sufficiently large to allow for the addition of dummy nodes to which unaligned nodes can formally be aligned.

**Value**

The return value is a permutation vector of the specified size.

**Author(s)**

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**Examples**

```
ex<-GenerateExample(dimA=22, dimB=22, filling=.5, covariance=.6,
  symmetric=TRUE, numOrths=10, correlated=seq(1,18))

pinitial<-InitialAlignment(psize=34, r=ex$r, mode="reciprocal")
```

InvertPermutation      *Invert permutation*

---

**Description**

Invert the permutation defined by the specified vector.

**Usage**

```
InvertPermutation(p)
```

**Arguments**

p                      permutation vector

**Details**

The return value is a permutation vector equal to the inverse of the input permutation.

**Author(s)**

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**Examples**

```
p <- rank(rnorm(10))
pInv <- InvertPermutation(p)
```

---

LinearAssignment      *Solve linear assignment problem*

---

**Description**

Solve the linear assignment problem specified by the cost matrix.

**Usage**

```
LinearAssignment(matrix)
```

**Arguments**

matrix                cost matrix

**Details**

This function solves the linear assignment problem defined by the input matrix. [Jonker, Volgenant 1987]



**Value**

The return value is a permutation vector equal to the solution of the linear assignment problem specified by the cost matrix. The result is the permutation P for which MP is minimal (where M is the cost matrix).

**Author(s)**

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**References**

Jonker, R & Volgenant, A. (1987) Computing 38, 325–340.

**Examples**

```
m <- matrix(rnorm(25), 5, 5)
px <- LinearAssignment(round(-1000 * (m / max(abs(m)))))
m[px,]
```

---

MatrixToBin

*Convert matrix to bin representation*

---

**Description**

Convert a matrix of real numbers to a vector of integer bin numbers according to the specified lookup vector.

**Usage**

```
MatrixToBin(M, lookup, clamp=TRUE)
```

**Arguments**

M	input matrix
lookup	lookup vector
clamp	clamp values to lookup range

**Details**

This function transforms a matrix of arbitrary values into a matrix of bin numbers corresponding to the data in the input matrix. Bin numbers are found using the specified lookup table (see [GetBin-Number](#)).

**Value**

The return value is a matrix containing the bin numbers for the elements of the input matrix.

**Author(s)**

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**Examples**

```
m <- matrix(rnorm(25), 5, 5)
lookup <- 0.2*(-5:5)
MatrixToBin(m, lookup)
```

---

Permute

*Permute rows and columns of a matrix*

---

**Description**

Permute rows and columns of the input matrix.

**Usage**

```
Permute(m, p, invertp=FALSE)
```

**Arguments**

m	matrix
p	permutation vector
invertp	apply inverse permutation

**Details**

This function permutes rows and columns of a matrix using the specified permutation vector. The inverse of the permutation will be applied if the invertp argument is set to TRUE.

**Value**

The return value is the row- and columnwise Permutation of the elements of the input matrix, so  $\text{Permute}(m, p)[i, j]$  is equal to  $m[p[i], p[j]]$ .

**Author(s)**

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**Examples**

```
example <- GenerateExample(10, 10, 1, 0.5, TRUE, 4)
b <- example$b
p <- rank(rnorm(10))
Permute(b, p, TRUE)
```

---

Trace	<i>Calculate trace of a matrix</i>
-------	------------------------------------

---

**Description**

Calculate the trace of a square matrix.

**Usage**

```
Trace(m)
```

**Arguments**

m	square matrix
---	---------------

**Details**

The return value is the trace of the input matrix.

**Author(s)**

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**Examples**

```
m <- matrix(c(1, 0, 0, 1), 2, 2)
Trace(m)
```

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VectorToBin	<i>Convert vector to bin representation</i>
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**Description**

Convert a vector of real numbers to a vector of integer bin numbers according to the specified lookup vector.

**Usage**

```
VectorToBin(v, lookup, clamp=TRUE)
```

**Arguments**

v	input vector
lookup	lookup vector
clamp	clamp values to lookup range

**Details**

This function transforms a vector of arbitrary values into a vector of bin numbers corresponding to the data in the input vector. Bin numbers are found using the specified lookup table (see [GetBinNumber](#)).

**Value**

The return value is a vector containing the bin numbers for the elements of the input vector.

**Author(s)**

Joern P. Meier, Michal Kolar, Ville Mustonen, Michael Laessig, and Johannes Berg

**Examples**

```
x <- rnorm(10)
lookup <- 0.2*(-5:5)
VectorToBin(x, lookup)
```

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